# **CSCI 275**: **Programming Abstractions Lecture 11: Higher Order Wrap-Up** Spring 2024

Stephen Checkoway, Oberlin College Slides gratefully borrowed from Molly Q Feldman





# **Questions?** Comments?

# Functional Language of the Week: Python

- Wait, hold on! Python is *not* a functional paradigm language • Paradigms are a gray area....
- The transition from Python 2 to Python 3 facilitated significantly better functional programming in Python • This was, more or less, due to popular demand

 A (long-running) guide to functional programming in Python https://docs.python.org/3/howto/functional.html#



# Functional Language of the Week: Python

#filter

x = filter(lambda x: x%3 == 0 and x%5 != 0, [3,6,9,12,15,18,21,24,27,30])
print(list(x)) #gives [3, 6, 9, 12, 18, 21, 24, 27]

#map

a = map(lambda x: x + 1, [1,2,3])
print(list(a)) #gives [2, 3, 4]

#subtle: how do you change how sorted works?
#a lambda!

r = sorted([(1,0), (2,1), (3,2)], key = lambda x: x[1])
print(list(r)) #gives [(1, 0), (2, 1), (3, 2)]



foldl

# **Reminder: Light Switch State Machine**

Possible actions: 'up, 'down, 'flip

**Possible states:** 'on, 'off

We want (state-after '(up flip)) => 'off

# Reminder: Lightswitch, as foldr and foldl

### (define state-after (lambda (actions) (foldr next-state 'off (reverse actions))))

(define (state-after-left actions) (foldl next-state 'off actions))

# foldl vs. foldr





return-value

### foldl combines elements of the list starting with the first (left-most) element

### foldr combines elements of the list starting with the last (right-most) element

# But wait: more "thoughtful" motivation for fold



# **Reminder: Tail Recursion and using an "accumulator"**

### (define (fact-a n acc) (if (<= n 1))acc ; return the accumulator (fact-a (sub1 n) (\* n acc)))) (define (fact2 n) (fact-a n 1))

### Four things to notice:

- We defined a recursive helper function that takes an additional param - We provide an initial value for the accumulator in fact2's call to fact-a - The base case returns the accumulator
- fact-a is tail-recursive





# **Product: An Accumulator Pattern**

(define (product-a lst acc) (cond [(empty? lst) acc] [else (product-a (rest lst)

(define (product lst) (product-a lst 1))

(\* (first lst) acc))]))



# **Reverse: An Accumulator Pattern**

(define (reverse-a lst acc) (cond [(empty? lst) acc] [else (reverse-a (rest lst) (cons (first lst) acc))]))

(define (reverse lst) (reverse-a lst empty))



# Map: An Accumulator Pattern

(define (map-a proc lst acc) (cond [(empty? lst) acc] [else (map-a proc (rest lst) (cons (proc (first lst)) acc))]))

(define (map proc lst) (reverse (map-a proc lst empty)))

# Accumulator Pattern

Basic structure is the same (rev (define (fun-a lst acc) (cond [(empty? lst) a [else (fun-a (rest l (combin (define (fun ... lst)

(fun-a lst initial-va

Function	initial-val	(combine head
product	1	(* head acc
reverse	empty	(cons head
map	empty	(cons (proc

Similarities		
writing slightly)		
LCC]		
.st) ne (first lst) acc))]))		
L ] )		
d acc)		
acc)		
head) acc)		
vve must reverse the resu		

# **Abstraction: fold left**

(foldl combine initial-val lst) combine:  $\alpha \times \beta \rightarrow \beta$ initial-val:  $\beta$ lst: list of  $\alpha$ fold:  $(\alpha \times \beta \rightarrow \beta) \times \beta \times (\text{list of } \alpha) \rightarrow \beta$ 

**Elements of** 1st =  $(x_1 x_2 \dots x_n)$  and initial-val are combined by computing  $z_1 = (combine x_1 initial-val)$  $z_2 = (combine x_2 z_1)$  $z_3 = (combine x_3 z_2)$  $z_n = (combine x_n z_{n-1})$ 





combine: number  $\times$  number  $\rightarrow$  number initial-val: number

lst: list of number





### reverse as fold left (foldl combine base-case lst) (define (reverse lst) (foldl cons empty lst))



combine:  $\alpha \times$  list of  $\alpha \rightarrow$  list of  $\alpha$ initial-val: list of  $\alpha$ lst: list of  $\alpha$ 



# Which fold to pick?

- "Most of the time", either will work +/- a call to reverse • Be careful when combine has ordering effects
- If the computation makes more sense as a right-to-left computation on the elements of the list, then use foldr
- But, most of the time, use foldl
  - Lists run left-to-right in Racket world
  - Fold in most other functional contexts assumes fold1 Tail recursive, and thus more efficient

Variable Argument Procedures

# Variable argument procedures (define foo (lambda params body))

bound to a list of the procedure's arguments

(define count-args (lambda params (length params)))

> Folks asked about why no parens worked in some previous homeworks, this is why!

- When params is a list of identifiers (as we know it thus far!), the identifiers are bound to the values of the procedure's arguments
- When params is an identifier (i.e., not a list), then the identifier is
  - (count-args 'a 2 #f) => 3



# **Required parameters + variable parameters**

(define foo (lambda (x y z . params)) body)

Separate the required parameters from the list of variable parameters with a period

(define drop-2 (lambda (x y . lst) lst))

(drop-2 1 2 3 4)

x is bound to 1 y is bound to 2 lst is bound to '(3 4)



# Review & Practice



# Potentially Helpful Baking Analogies





You are making cherry cookies. You need have the dough on the pan. You then need to put a cherry in the middle of every cookie.

You are the Cookie Monster. You have a big pile of cookies and you're eating them all.



# apply



### foldl/r

You are making meringue. An important step is to fold in air to make it light and fluffy. Each turn of the spatula adds more air!



There's a standard library procedure (round x) that takes a number as input and rounds it to the nearest integer.

If we have a list of numbers ' (1.1 2.9 3.5 4.0) and we want a list of rounded numbers ' (1.0 3.0 4.0 4.0), how can we get that?

A.(map (round x) '(1.1 2.9 3.5 4.0))
B.(map (lambda (x) (round x)) '(1.1 2.9 3.5 4.0))
C.(map round '(1.1 2.9 3.5 4.0))
D.(round '(1.1 2.9 3.5 4.0))
E.More than one of the above



# Distance of a 2-d point from the origin

- Recall that a point (x, y) lie
- Let's make a procedure to compute this (define (distance-from-origin x y) (sqrt (+ (\* x x) (\* y y)))
- (distance-from-origin 3 4) => 5

es 
$$\sqrt{x^2 + y^2}$$
 from the origin

(define (distance-from-origin x y) (sqrt (+ (\* x x) (\* y y)))) If we have a point (define p '(5 -8)) how can we get its distance from the origin?

A. (distance-from-origin p)

B. (apply distance-from-origin p)

D.More than one of the above

- C. (distance-from-origin (first p) (second p))



# Shapes

Racket library 2htdp/image has procedures for creating images

(require 2htdp/image) (circle 20 'solid 'red) => radius (rectangle 50 20 'outline 'blue) => height



If we have a list of radii, say lst is '(20 30 50 60) and we want a list of solid, red circles with those radii, which should we use? A. (map circle 'solid 'red lst) B. (map (lambda (r) (circle r 'solid 'red)) lst) C. (apply circle 'solid 'red lst) D. (apply (lambda (r) (circle r 'solid 'red)) lst) E. (foldr (lambda (r) (circle r 'solid 'red)) empty lst)





# **Combining images**

(empty-scene 320 180) **gives a v** draw on

(place-image img x y scene) returns a new image by starting with scene and drawing img at (x, y)

(let\* ([c (circle 40 'solid 'blue)]
 [r (rectangle 200 30 'solid 'red)]

- [s0 (empty-scene 320 180)]
- [s1 (place-image c 50 90 s0)]
- [s2 (place-image r 150 90 s1)]
- [s3 (place-image c 180 70 s2)])

### (empty-scene 320 180) gives a white rectangle with a black border we can

```
'blue)]
'solid 'red
180)]
90 s0)]
0 90 s1)]
0 70 s2)])
```



Imagine we have a list of 3-element lists (shape x y), e.g., 1st is the list (list (list (circle 40 'solid 'blue) 50 90) (list (rectangle 200 30 'solid 'red) 150 90) (list (circle 40 'solid 'purple) 180 70))

How would you draw those shapes on a scene at their coordinates? A. (map (lambda (i) (place-image (first i) (second i) (third i) scene))

lst)

B. (apply (lambda (i) (place-image (first i) (second i) (third i) scene))

lst)

C. (foldr (lambda (i s) (place-image (first i) (second i) (third i) s))

scene lst)

# Try out the previous question on your own!